1986 NYSML 73

RELAY 1

- R1-1. Compute the integer N, where (3!)(5!)(7!) = N!
- R1-2. Let t be TNYWR. In isosceles triangle ABC, base BC = t and angle $A = 36^{\circ}$. Compute the length of the bisector of angle B.
- R1-3. Let t be TNYWR. Compute the tens digit of $(1985)(1986)(1987)^t$.
- R1-4. Let t be TNYWR. If 4a = 5b = 6c, compute the ratio of the integers a:b:c, where a, b, and c are the smallest possible set of positive integers with this property.

PASS BACK THE INTEGER
$$\frac{a+b+c+8}{t}$$
.

R1-5. Let t be TNYWR. The roots of $tx^2 - 7x + k = 0$ are sin A and cos A. Compute the numerical value of k.

RELAY 2

- R2-1. How many 2-digit numbers, neither of whose digits is 0, are such that the product of their digits is a square?
- R2-2. Let t be TNYWR. If x and y are real and |x + y t| + |x y 5| = 0, compute the numerical value of y.
- R2-3. Let t be TNYWR. The graph of y = f(x) is symmetric about the line x = 4 and about the point (8,t). If (3,7) is on the graph, then (11,k) must also be on the graph. Compute k.
- R2-4. Let t be TNYWR. The 4-digit (base 10) numeral $\underline{A} \ \underline{3} \ \underline{t} \ \underline{B}$ is a multiple of 99. Compute the digit \underline{A} .
- R2-5. Let t be TNYWR. In triangle ABC, $\cos A = \frac{t}{5}$ and $\cos B = \frac{5}{13}$. Compute $\cos C$.