

an integral multiple of the smallest subscript in the set. For example,  $\{a_2, a_6, a_8\}$  is an acceptable set, as is  $\{a_8\}$ . How many such sets can be formed?

### INDIVIDUAL QUESTIONS

- I1. Compute  $n$  if  $(10^{12} + 25)^2 - (10^{12} - 25)^2 = 10^n$ .
- I2. If  $0^\circ < x < 90^\circ$  and  $\cos x = \frac{3}{\sqrt{10}}$ , compute  $\log \sin x + \log \cos x + \log \tan x$ .
- I3. The integers  $x$ ,  $y$ , and  $z$  are each perfect squares, and  $x > y > z > 0$ . If  $x$ ,  $y$ , and  $z$  form an arithmetic progression, compute the smallest possible value of  $x$ .
- I4. In triangle  $ABC$ , altitude  $\overline{AH}$  and median  $\overline{BM}$  intersect inside the triangle and are equal. If  $\sphericalangle ACB = 41^\circ$ , find the measure of  $\sphericalangle MBC$ .
- I5. There are exactly four positive integers  $n$  such that  $\frac{(n+1)^2}{n+23}$  is an integer. Compute the largest such  $n$ .
- I6. In triangle  $ABC$ ,  $P$  and  $Q$  are the midpoints of  $\overline{AB}$  and  $\overline{AC}$  respectively;  $R$  and  $S$  are the trisection points of  $\overline{BC}$  (with  $R$  closer to  $B$ ).  $\overline{PS}$  and  $\overline{QR}$  intersect in  $T$ . If the area of triangle  $ABC$  is 60, compute the area of triangle  $PQT$ .

### RELAY 1

- R1-1. In the diagram,  $O$  is the center of the circle,  $\overline{CE} \cong \overline{ED}$  in triangle  $CED$ , and  $\sphericalangle AOB$  is a right angle, as shown. If the ratio of the area of  $\triangle CED$  to the area of  $\triangle AOB$  is  $k:1$ , compute  $k$ .

