

**RELAY #1**

R1-1. The product of five consecutive positive integers is divisible by both 13 and 31. If that product is as small as possible, compute the smallest of the five integers.

R1-2. Let  $T = \text{TNYWR}$  and let  $K = \frac{T-1}{15}$ .  
Compute the value of  $(1 - i)^{2K}$ .

R1-3. Let  $T = \text{TNYWR}$ .

Three vertices of a cube are connected to form a triangle. Compute the maximum possible perimeter for this triangle if the edge of the cube is  $T$ .

**Relay #2**

R2-1. Compute the largest integer less than 125 that has a prime number of distinct (positive) factors.

R2-2. Let  $T = \text{TNYWR}$  and let  $K = T/11$ .  
If  $\log_n 2 = K$ , and  $n > 1$ , compute  $\log_4 n$ .

R2-3. Let  $T = \text{TNYWR}$  and let  $r = 1/T$ .  
For integer  $n \geq 0$ ,  $F(n + 1) = x \cdot F(n) + 1$ , and  $F(0) = 1$ .  
Express  $(x - 1) \cdot F(r)$  as a polynomial in  $x$  with integer coefficients.

[Note: The answer is *not* to be expressed in factored form, and is to be simplified as much as possible!]